

Thermodynamic Processes

- States of a thermodynamic system can be changed by interacting with its surrounding through work and heat. When this change occurs in a system, it is said that the system is undergoing a **process**.
- A thermodynamic **cycle** is a sequence of different processes that begins and ends at the same thermodynamic state.
- Some sample processes:
 - ➔ Isothermal process: temperature is constant $T=C$
 - ➔ Isobaric process: pressure is constant, $P=C$
 - ➔ Isentropic process: entropy is constant, $s=C$
 - ➔ Constant-volume process, $v=C$
 - ➔ Adiabatic process: no heat transfer, $Q=0$

Process-1

- Use ideal gas assumption (closed system):

→ Isothermal process: $T = \text{constant}$

Energy balance $\Delta U = Q - W$, for ideal gas $\Delta U = \Delta H = 0$
since both are functions of temperature only

$$Q = W, \quad W = \int P dV = \int \frac{mRT}{V} dV = mRT \int_1^2 \frac{dV}{V}$$

$$= mRT \ln \left(\frac{V_2}{V_1} \right) = mRT \ln \left(\frac{P_1}{P_2} \right)$$

→ Isobaric process: $P = \text{constant}$

$$\Delta U = Q - W, \quad W = \int P dV = P \int_1^2 dV = P(V_2 - V_1)$$

$$Q = \Delta U + P(V_2 - V_1) = (U_2 - U_1) + P(V_2 - V_1)$$
$$= (U_2 + PV_2) - (U_1 + PV_1) = H_2 - H_1 = \Delta H$$

Process-2

→ Constant volume process: $V = \text{constant}$

$$Q - W = \Delta U, \quad W = \int P dV = 0, \quad \text{no work done}$$

$$Q = \Delta U = m \Delta u = m \int c_v dT$$

→ Adiabatic process: $Q = 0$

$$Q - W = \Delta U, \quad -W = \Delta U$$

$-\delta W = dU$ (infinitesimal increment of work and energy)

$$dU + PdV = 0, \quad mc_v dT + \left(\frac{mRT}{V} \right) dV = 0$$

$$c_v dT + \left(\frac{RT}{V} \right) dV = 0, \quad \frac{c_v}{R} \frac{dT}{T} = -\frac{dV}{V}, \quad \text{integrate and assume}$$

$c_v = \text{constant}$

$$\frac{c_v}{R} \ln \left(\frac{T_2}{T_1} \right) = -\ln \left(\frac{V_2}{V_1} \right), \quad \frac{T_2}{T_1} = \left(\frac{V_1}{V_2} \right)^{R/c_v} = \left(\frac{V_1}{V_2} \right)^{k-1}$$

Process-3

$$\frac{T_2}{T_1} = \left(\frac{V_1}{V_2} \right)^{k-1}, \text{ from ideal gas relation}$$

$$PV=RT, \left(\frac{V_1}{V_2} \right) = \left(\frac{T_1}{T_2} \right) \frac{P_2}{P_1}, \text{ substitute}$$

$$\frac{T_2}{T_1} = \left(\left(\frac{T_1}{T_2} \right) \left(\frac{P_2}{P_1} \right) \right)^{k-1}, \text{ multiply } \left(\frac{T_2}{T_1} \right)^{k-1} \text{ from both sides}$$

$$\frac{T_2}{T_1} = \left(\frac{P_2}{P_1} \right)^{\frac{(k-1)}{k}}, \text{ and } \left(\frac{P_2}{P_1} \right) = \left(\frac{V_1}{V_2} \right)^k$$

Also $P_1 V_1^k = P_2 V_2^k$ and $pV^k = \text{constant}$

For an ideal gas undergoing adiabatic process

Process-4

Polytropic Process: its P-V relation can be expressed as

$PV^n = \text{constant}$, where n is a constant for a specific process

- Isothermal, $T = \text{constant}$, if the gas is an ideal gas then $PV = RT = \text{constant}$, $n = 1$
- Isobaric, $P = \text{constant}$, $n = 0$ (for all substances)
- Constant-volume, $V = \text{constant}$, $V = \text{constant}(P)^{(1/n)}$, $n = \infty$ (for all substances)
- Adiabatic process, $n = k$ for an ideal gas

$$P_1 V_1^n = P_2 V_2^n = PV^n$$

$$W = \int_1^2 P dV = \int_1^2 (P_1 V_1^n) V^{-n} dV$$

$$= (P_1 V_1^n) \int_1^2 V^{-n} dV = \frac{(P_1 V_1^n)}{1-n} (V_2^{1-n} - V_1^{1-n}) = \frac{P_2 V_2 - P_1 V_1}{1-n}$$